

# CS210 Data Structures (181) Final Exam

Name: \_\_\_\_\_ ID \_\_\_\_\_

## Instructions:

- This exam contains four questions with multiple parts.
- Time allowed: 180 minutes
- Closed Book, Closed Notes.
- There are 12 pages in this exam booklet.
- **Use of Calculators and / or computing devices / smartphones etc is strictly prohibited.**
- Answer the problems on the exam sheets only. No additional attachments would be accepted.
- When the “time is over” is called, it is students responsibility to submit his exam to the invigilator. Submitting completed exam 3 minutes after the “time is over” will incur a penalty of 5 points.

## Few gentle reminders:

- If you get stuck on some problem for a long time, move on to the next one.
- The ordering of the problems is somewhat related to their relative difficulty. However, the order might be different for you!
- You should be better off by first reading all questions and answering them in the order of what you think is the easiest to the hardest problem.
- Keep the points distribution in mind when deciding how much time to spend on each problem.

Do not write below this:

Q1	Q2	Q3	Q4	Total:/40
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## CLO Assessment

CLO1 – Q1(10)	CLO2 – Q2 (10)	CLO3 – Q3 (16)	CLO4 – Q4 (4)
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**Question1 [CLO 1]: [ /10 Points]**

**1-A). State the runtime requirements in big-O for each of the following code fragments. [ /2.0]**

	Code Fragment	Running Time in big-O
<b>a</b>	<pre>int a = 0; for (i = 0; i &lt; n; i++) {     for (j = 0; j &lt; i; j++) {         a = a + i + j;     } }</pre>	
<b>b</b>	<pre>function(int n) {     if (n==1)         return 0;     else         return 1 + function(n-1); }</pre>	
<b>c</b>	<pre>int a = 0, i = n; do {     a += i;     i /= 2; } while (i &gt; 0);</pre>	
<b>d</b>	<pre>int n = N; for(int p=0;p&lt;N;p++) {     while (1){         if(n&gt;0){             n = n/2;         }else             break;     }     n = N; }</pre>	

**1-B). Read the statement and circle the appropriate choice of data structure. [ /2.0]**

Problem	Answer
<p>A method that reads a list of names and prints all the names in the opposite order</p> <p>a. Priority Queue b. Stack c. Binary Tree d. minHeap</p>	
<p>A method that arranges the patients names according to the severity of injuries in a hospital emergency room.</p> <p>a. MaxHeap b. Hash table c. Priority Queue d. Queue</p>	
<p>A graph storage mechanism that ensures a constant run-time to find an edge that may or may not exist in the graph.</p> <p>a. Adjacency list b. Adjacency matrix c. Edge list d. None of the above</p>	
<p>A mechanism that allows sorting all courses in your schedule based on the pre-requisite.</p> <p>a. DiGraph b. DAG c. Depth First Search d. Topological sort</p>	

**1-C). Draw a binary tree with these conditions:**

[ /2.0]

Draw a binary tree with these conditions:

Each node in the tree stores only one character

The in-order traversal of this tree gives:

**C O T T O N C A N D Y**

The post-order traversal of this tree gives:

**C O T O N A Y D N C T**

**1-D). Insert the following keys in a priority queue (minHeap); show all insertions, sink and swim operations.**

[ /2.0]

10 7 8 25 5 11 2

**1-E). Remove two keys from the above heap. Show all sink swim operations**

[ /2.0]

**Question2 [CLO 2]: [ \_\_\_ /10 Points]**

**2-A). Show the sort operations of a bottom-up merge sort for the following keys. Use standard order of alphabets for sorting (A to Z).**

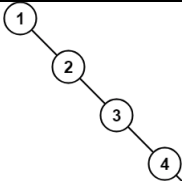
[ \_\_\_ /4.0]

cat	cam	and	zed	bad	arm	bbd	bam	abd	dad	jar	pat	car
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----

ABCDEFGHIJKLMNOPQRSTUVWXYZ

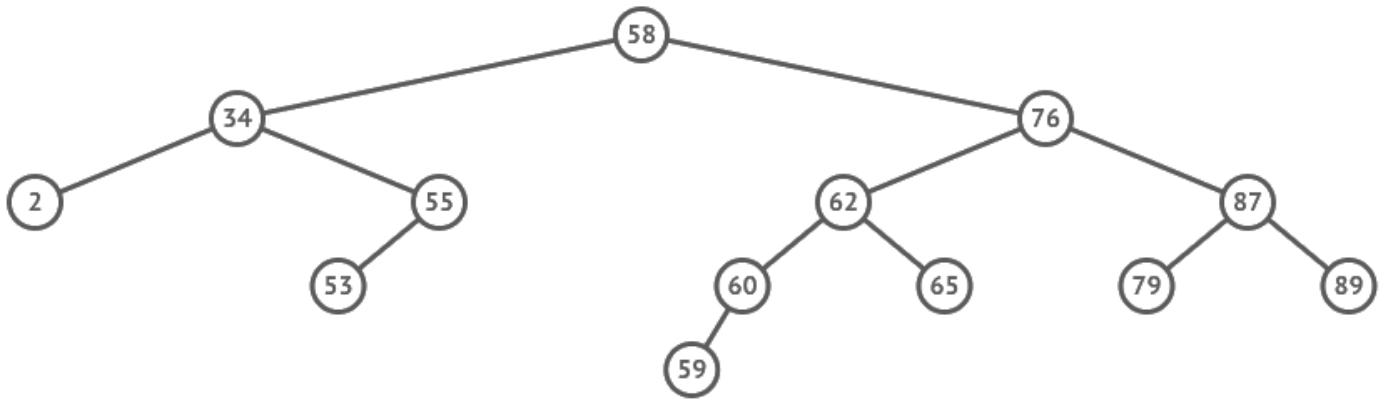
2-B). Read the statement and write the appropriate choice in the box provided

[ /3.0]

Problem	Answer
<p>Which sorting algorithm will take the least time (number of comparisons) when all elements of input array are identical? Consider typical implementations of sorting algorithms.</p> <ol style="list-style-type: none"> <li>Insertion Sort</li> <li>Heap Sort</li> <li>Merge Sort</li> <li>Selection Sort</li> </ol>	
<p>Assume an array of integers = {2, 4, 3, 1, 6}; applying quick sort, which values would be selected as pivots</p> <ol style="list-style-type: none"> <li>2 and 1</li> <li>2 and 4</li> <li>3 and 6</li> <li>3 and 1</li> </ol>	
<p>Which of the following is not a stable sorting algorithm in its typical implementation.</p> <ol style="list-style-type: none"> <li>Merge sort</li> <li>Quick sort</li> <li>Insertion sort</li> <li>None of the above</li> </ol>	
<p>Which sorting algorithm gives <math>O(n^2)</math> comparisons and <math>O(n)</math> swaps for random data?</p> <ol style="list-style-type: none"> <li>Quick sort</li> <li>Insertion sort</li> <li>Merge sort</li> <li>Selection sort</li> </ol>	
<p>The run-time for searching a key in a skewed Binary Search Tree is</p> <ol style="list-style-type: none"> <li><math>O(n)</math></li> <li><math>O(\log n)</math></li> <li><math>O(1)</math></li> <li><math>O(n^2)</math></li> </ol>	
<p>Which of the following is an inappropriate search sequence for 36 in a BST composed of integers?</p> <ol style="list-style-type: none"> <li>93, 27, 34, 62, 99, 36</li> <li>11, 22, 33, 40, 35, 36</li> <li>23, 48, 42, 40, 33, 36</li> <li>11, 12, 13, 14, 25, 36</li> </ol>	

2-C). Identify all rotations to remove 2 from the following AVL Tree.

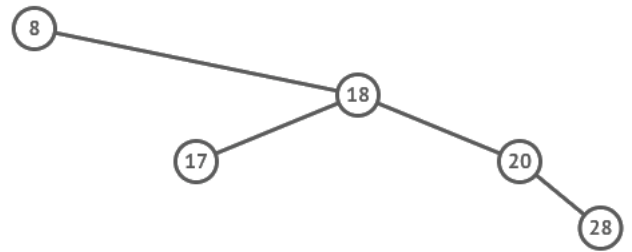
[ /3.0]



**Question3 [CLO 3]: [ \_\_\_ /16 Points]**

3-A). Give pseudocode for a method called ancestors for a BST node P. This BST stores nodes with keys of type integers. It prints all the parent, grand-parent, grand-grand-parent etc keys on console. If a P has no ancestors, it prints -1.

[ \_\_\_ /3.0]



**Example: Ancestors of P=28 are: 20, 18, and 8.**



3-B). Give code for a method called degree. This method takes two parameters, an undirected Graph G represented by a 2-dimensional Array (Adjacency matrix) and an integer V representing a vertex in graph G. This method counts and returns the number of edges connected to vertex V.

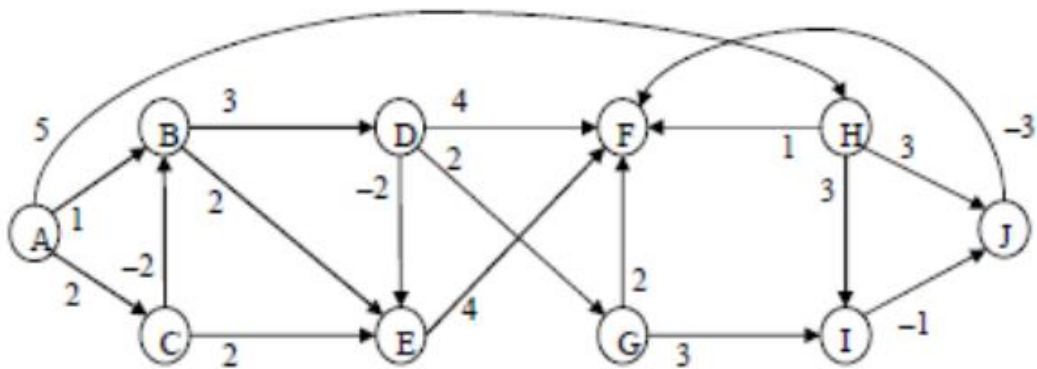
[ /3.0]

```
public int degree(Graph G, int v) {
```

	1	2	3
1	0	1	0
2	1	0	1
3	0	1	0

3-C). For the following DiGraph provide an Adjacency list.

[ /2.0]



A
B
C
D
E
F
G
H
I
J

3-D). For the above graph, show a Breadth First Search (BFS) run starting at A. Consider lowest weights for traversal. Use appropriate Data Structures.

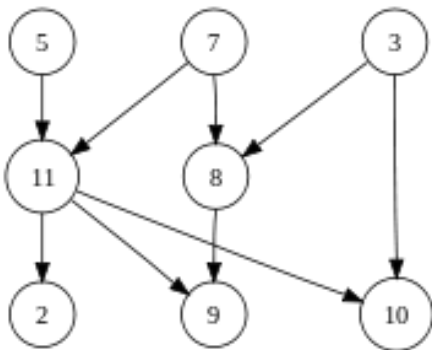
[ /2.0]

3-E). Given a DiGraph G with V vertices and E edges. Give a brute force algorithm that finds all possible paths from a source S to a destination D using BFS. What is the run-time for this algorithm?

[ /3.0]

3-F). For the graph shown below, provide the result of a DFS based topological sort algorithm starting at 3. Show the content of the extra stack used.

[ /3.0]



**Question4 [CLO 4]: [ \_\_\_ /4 Points]**

4). Given input {4373, 1323, 6173, 4194, 4345, 9673, 1983, 2106, 3909}, a hash table A of size 10 and a hash function  $h(x) = x \text{ mod } 10$ , show the resulting hash map using each of the following collision resolution methods:

[ \_\_\_ /4.0]

Separate chaining hash table.

A

x	$h(x) = x \text{ mod } 10$

0	
1	
2	
3	
4	
5	
6	
7	
8	
9	

Hash table using linear probing.

A

0	1	2	3	4	5	6	7	8	9

How many collisions?

How many displacements?

--End of Exam--